

Compiler concepts: Parsing

COMSM1302 Overview of Computer Architecture

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Describing languages

We have a description of Hack syntax in Nisan and Schocken, right?

A more sophisticated approach

We'll need a highly sophisticated mathematical construction:

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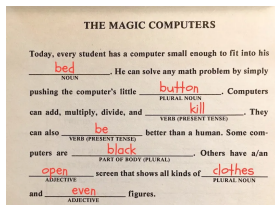
THE MAGIC COMPUTERS

Today, every student has a computer small enough to fit into his
_____ **bed** _____. He can solve any math problem by simply
NOUN
pushing the computer's little _____ **button** _____. Computers
PLURAL NOUN
can add, multiply, divide, and _____ **kill** _____. They
VERB (PRESENT TENSE)
can also _____ **be** _____ better than a human. Some com-
VERB (PRESENT TENSE)
puters are _____ **black** _____. Others have a/an
PART OF BODY (PLURAL)
_____ **open** _____ screen that shows all kinds of _____ **clothes** _____.
ADJECTIVE PLURAL NOUN
and _____ **even** _____ figures.
ADJECTIVE

Source: Jesse Vig via Medium ([here](#))

A more sophisticated approach: Madlibs?

We'll need a highly sophisticated mathematical construction: Madlibs.



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A **context-free grammar** (or just **grammar**) is a way of quickly and rigorously specifying which strings in a language have valid syntax.

There is a deep and rich mathematical theory here, which we thankfully don't need to learn! Programmers express grammars in **Backus-Naur Form (BNF)**, and usually just understanding BNF is enough.

BNF is basically Madlibs, but recursive.

Introduction to ~~Madlib~~s Backus-Naur Form (BNF)

Here's a simple example:

$$\langle \text{noun} \rangle ::= \text{'lecturer'} \mid \text{'student'} \mid \text{'pizza'}$$
$$\langle \text{presentVerb} \rangle ::= \text{'eats'} \mid \text{'devours'} \mid \text{'consumes'}$$

You can read each \mid as “or” and each $::=$ as “is defined as”. E.g. a $\langle \text{noun} \rangle$ is defined as one of the three strings ‘lecturer’, ‘student’, or ‘pizza’.

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We can also build up definitions in terms of other definitions, e.g.

$$\langle \text{sentence} \rangle ::= \text{'The'} \langle \text{noun} \rangle \langle \text{presentVerb} \rangle \text{'the'} \langle \text{noun} \rangle$$

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‘The’ **‘lecturer’** **‘consumes’** ‘the’ **‘pizza’**

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Anything we define as part of the grammar must be enclosed in $\langle \rangle$ s. We call these **non-terminal symbols**. Anything else (e.g. ‘lecturer’) is a **terminal symbol** or **token**.

Example: Integers

The last feature of BNF is the source of its power: it allows **recursion**.

For example, suppose our tokens are '0' through '9', and we want to define a non-terminal symbol that matches precisely the non-negative whole numbers (allowing for leading zeroes). We could write:

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$$\begin{aligned}\langle \text{digit} \rangle &::= '0' \mid '1' \mid '2' \mid '3' \mid '4' \mid '5' \mid '6' \mid '7' \mid '8' \mid '9' \\ \langle \text{number} \rangle &::= \langle \text{digit} \rangle \mid \langle \text{digit} \rangle \langle \text{number} \rangle\end{aligned}$$

E.g. '016' is a $\langle \text{number} \rangle$ because we can expand $\langle \text{number} \rangle$'s definition as:

$$\begin{aligned}\langle \text{number} \rangle &\longrightarrow \langle \text{digit} \rangle \langle \text{number} \rangle \longrightarrow \langle \text{digit} \rangle \langle \text{digit} \rangle \langle \text{number} \rangle \\ &\longrightarrow \langle \text{digit} \rangle \langle \text{digit} \rangle \langle \text{digit} \rangle \longrightarrow '0' '1' '6' .\end{aligned}$$

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That's it! That's all of BNF. It can be hard to use and hard to reason about, but the syntax is simple.

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How should we redefine $\langle \text{number} \rangle$ to allow negative numbers, but forbid leading zeroes? (Assume we have '0' through '9' and '-' as tokens.)

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Some sanity checks for any such re-definition:

- '-' '1' '0' should be a $\langle \text{number} \rangle$.
- '0' should be a $\langle \text{number} \rangle$.
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There are multiple approaches — there's no such thing as the “right” expression of a grammar in BNF. Here's one way:

$$\langle \text{posDigit} \rangle ::= '1' \mid '2' \mid '3' \mid '4' \mid '5' \mid '6' \mid '7' \mid '8' \mid '9'$$
$$\langle \text{posNumber} \rangle ::= \langle \text{posDigit} \rangle \mid \langle \text{posNumber} \rangle \langle \text{posDigit} \rangle \mid \langle \text{posNumber} \rangle '0'$$
$$\langle \text{number} \rangle ::= \langle \text{posNumber} \rangle \mid '0' \mid '-' \langle \text{posNumber} \rangle$$

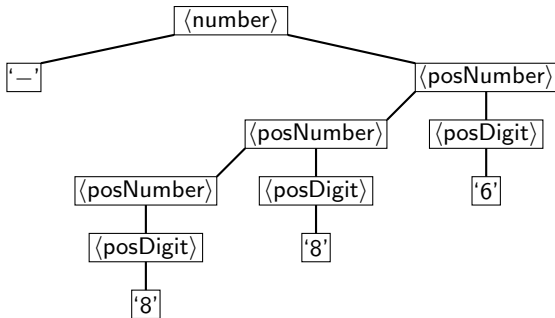
Parse trees

$\langle \text{posDigit} \rangle ::= '1' \mid '2' \mid '3' \mid '4' \mid '5' \mid '6' \mid '7' \mid '8' \mid '9'$

$\langle \text{posNumber} \rangle ::= \langle \text{posDigit} \rangle \mid \langle \text{posNumber} \rangle \langle \text{posDigit} \rangle \mid \langle \text{posNumber} \rangle '0'$

$\langle \text{number} \rangle ::= \langle \text{posNumber} \rangle \mid '0' \mid '-' \langle \text{posNumber} \rangle$

The goal of parsing is to convert a list of tokens into a **parse tree** or **concrete syntax tree (CST)** which gives its BNF structure. E.g. for “-886”:



Each non-terminal symbol is a node. Its children are its BNF expansion, in order from left to right — so the leaves are precisely the tokens.

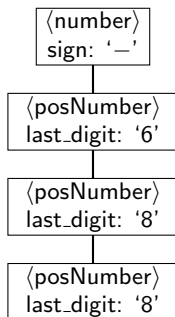
Abstract syntax trees

$\langle \text{posDigit} \rangle ::= '1' \mid '2' \mid '3' \mid '4' \mid '5' \mid '6' \mid '7' \mid '8' \mid '9'$

$\langle \text{posNumber} \rangle ::= \langle \text{posDigit} \rangle \mid \langle \text{posNumber} \rangle \langle \text{posDigit} \rangle \mid \langle \text{posNumber} \rangle '0'$

$\langle \text{number} \rangle ::= \langle \text{posNumber} \rangle \mid '0' \mid '-' \langle \text{posNumber} \rangle$

For efficiency and convenience, we may choose to process a CST into an **abstract syntax tree (AST)**, which contains the same information in a more convenient form. E.g. we might decide we don't need the $\langle \text{posDigit} \rangle$ nodes:



Consider this grammar for simple arithmetic expressions.

$$\langle \text{expression} \rangle ::= \langle \text{number} \rangle \mid \langle \text{expression} \rangle \langle \text{operator} \rangle \langle \text{expression} \rangle \mid$$
$$\quad \quad \quad \langle ' \langle \text{expression} \rangle \langle \text{operator} \rangle \langle \text{expression} \rangle ' \rangle$$
$$\langle \text{operator} \rangle ::= '+' \mid '-' \mid '*' \mid '/' \mid '^'$$

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$$\begin{aligned}\langle \text{expression} \rangle &::= \langle \text{number} \rangle \mid \langle \text{expression} \rangle \langle \text{operator} \rangle \langle \text{expression} \rangle \mid \\ &\quad \text{'('} \langle \text{expression} \rangle \langle \text{operator} \rangle \langle \text{expression} \rangle \text{'}' \\ \langle \text{operator} \rangle &::= \text{'+'} \mid \text{'-'} \mid \text{'*'} \mid \text{'/'} \mid \text{'^'}\end{aligned}$$

Then a parser could output several valid CSTs for e.g. $(3 + 4) * (5 - 1) / 3$.

This **ambiguity** can be dealt with *as long as* the semantic meaning is not ambiguous. E.g. here it is the same for all CSTs.

Generating parse trees

Parsing is a difficult and subtle problem, but a well-understood one.

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NOOOOOOOOOOOO!!!! YOU
CANT HAVE THE COMPUTER WRITE YOUR
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NON-CONTEXT-FREE GRAMMARS AND
RECURSIVE DESCENT AND ALL THE BEAUTIFUL
SUBTLETY OF TYPE THEORY NOOOOOOOOOOOOOO



haha yacc
go brrrrrrrr

Source: Generated with imgflip ([here](#)).

This means we shouldn't try to solve it again ourselves! We should instead use a **parser generator** which takes our grammar in BNF form and outputs code for a parser in a language of our choice. (E.g. yacc for C.)

Extended Backus-Naur Form (EBNF)

Often both parser generators and language specifications add extra syntax to BNF for usability, but there's no one standard. Based loosely on ISO 14977, we'll add:

- $()$ s mean grouped terms, e.g. $('0' \mid '1') ('0' \mid '1')$ means 00, 01, 10 or 11.
- $[]$ s mean optional terms, e.g. $['0'] '1'$ means 01 or 1.
- $\{ \}$ s mean repetition, e.g. $\{ '0' \mid '1' \}$ means any number of zeroes and ones (including the empty string).
- $A - B$ means anything that matches A , but doesn't match B , e.g. $\langle \text{number} \rangle - \langle \text{posNumber} \rangle$ means any number that's not a $\langle \text{posNumber} \rangle$.

This doesn't let BNF express any grammars it couldn't before (why not?), but it does make it much nicer to read and write. For example:

$$\begin{aligned} \langle \text{digit} \rangle &::= '0' \mid '1' \mid '2' \mid '3' \mid '4' \mid '5' \mid '6' \mid '7' \mid '8' \mid '9' \\ \langle \text{number} \rangle &::= (['-'] (\langle \text{digit} \rangle - '0') \{ \langle \text{digit} \rangle \}) \mid '0' \end{aligned}$$

With EBNF, we can build a readable grammar for all of C, never mind Hack! See for example [here](#) (credit Samuya Debray).